

# Field- and current-driven domain wall dynamics: An experimental picture

G.S.D. Beach<sup>\*</sup>, C. Knutson, M. Tsoi, J.L. Erskine

Department of Physics, The University of Texas at Austin, Austin, TX 78712-0264, USA

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## Abstract

Field- and current-driven domain wall velocities are measured and discussed in terms of existing spin-torque models. A reversal in the roles of adiabatic and non-adiabatic spin-torque is shown to arise in those models below and above Walker breakdown. The measured dependence of velocity on current is the same in both regimes, indicating both spin-torque components have similar magnitude. However, the models on which these conclusions are based have serious quantitative shortcomings in describing the observed field-driven wall dynamics, for which they were originally developed. Hence, the applicability of simple one-dimensional models to most experimental conditions may be limited.

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The capacity of a spin-polarized current to move a domain wall is experimentally well established [1–3], but the mechanisms responsible for that motion [4–9] remain under debate. Models fall into two classes, termed “adiabatic” [4–6] and “non-adiabatic” [5,7–9]. Most analytical work has cast these interactions within the framework of one-dimensional (1D) domain wall dynamics formulated decades ago [10]. Here we outline the predicted wall dynamics, present experimental characterizations of these dynamics, and discuss them in terms of the 1D models. Interpretation of the data within a 1D model framework provides estimates of relevant spin-torque parameters. However, the same model predicts key parameters of field-driven motion at odds with experiment by up to three orders of magnitude. The quantitative failure of the 1D model to describe field-driven motion warrants caution in directly extending the model to current-driven motion.

A wall geometry appropriate for most recent experiments [2,3] is shown in Fig. 1. The orientation of each spin

is denoted  $(\theta, \phi)$ , and  $\theta(x)$  varies from 0 to  $\pi$  over a characteristic width  $\Delta$  [10]. The wall is described by two collective coordinates derived from  $\theta$  and  $\phi$ : the wall displacement  $q$  and its canting angle  $\psi$ . Wall motion requires a torque on  $\theta$  to bring the wall spins toward the applied field  $H_a$ . However,  $H_a$  applies a torque not to  $\theta$ , but to  $\phi$ , and thus cannot directly drive wall motion. Instead,  $H_a$  cants  $\psi$  away from the easy plane and a demagnetizing field  $H_d$  develops. It is the demagnetizing torque,  $\gamma \vec{M} \times \vec{H}_d$ , that drives  $\theta$  and consequent wall motion  $\dot{q}$ . The existence of a velocity maximum [10] then follows naturally. At  $\psi = \pi/4$ , the demagnetizing torque, and thus  $\dot{q}$ , peaks. If  $H_a$  drives  $\psi$  past this limit,  $\psi$  can no longer remain

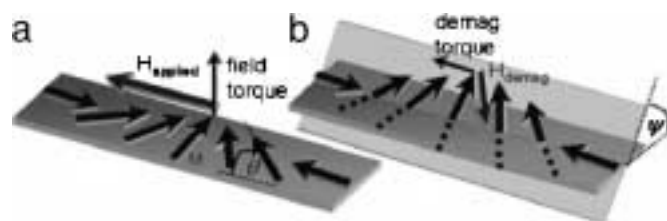


Fig. 1. Domain wall subjected to an axial field.

<sup>\*</sup>Corresponding author. Tel.: +1 512 471 7073; fax: +1 512 471 6518.  
E-mail address: [gbeach@physics.utexas.edu](mailto:gbeach@physics.utexas.edu) (G.S.D. Beach).

stationary, a transition termed Walker breakdown.  $\psi$  advances continually and the demagnetizing torque contribution to  $\dot{\mathbf{q}}$ ,  $(\gamma\vec{M} \times \vec{H}_d)$ , changes direction with each quarter period, averaging to zero.  $\psi$  rotation becomes more rapid with increasing  $H_a$ , leading to a small net damping torque  $(\alpha\vec{M} \times \dot{\mathbf{M}})$  that cants the wall spins toward  $H_a$  and drives the wall forward. At high  $H_a$ , this damping torque provides the sole contribution to  $\dot{\mathbf{q}}$ .

In this picture, the roles of adiabatic and non-adiabatic spin-torque are, loosely, to drive  $\psi$  and  $\mathbf{q}$  motion, respectively, and the following equations of motion emerge [5,9]:

$$\dot{\mathbf{q}} = (2\pi\mathbf{M}_s)\gamma \Delta \sin 2\psi + \alpha \Delta \dot{\psi} + \eta \mathbf{u}, \quad (1a)$$

$$\dot{\psi} = \gamma H_a - (\alpha/\Delta)\dot{\mathbf{q}} + (\beta\mathbf{u})/\Delta. \quad (1b)$$

A current density  $\mathbf{j}$  is included via  $\mathbf{u} = -(\mathbf{g}\mu_B\mathbf{p}/2eM_s)\mathbf{j}$  [11].  $\beta$  defines the strength of the non-adiabatic interaction, appearing in Eq. (1b), and is expected to be  $\sim 10^{-2}$  [8,9]. Adiabatic torque appears in Eq. (1a), with  $\eta \equiv 1$  in most models. There are two limiting cases, which occur below and far above breakdown: (I)  $\dot{\psi} = 0$  and (II)  $\dot{\psi} \gg 1$ . The first represents stationary motion wherein  $\dot{\mathbf{q}}$  is dictated by Eq. (1b),

$$\dot{\mathbf{q}}_I = (\gamma\Delta/\alpha)H_a + (\beta\mathbf{u})/\alpha. \quad (2)$$

Only the non-adiabatic term drives wall motion.  $\psi$  must adapt to maintain equality between Eqs. 1(a and b), and the sole effect of adiabatic torque is to shift the steady-state  $\psi$ . Stationary motion exists only up to  $\psi = \pi/4$ , which occurs at

$$H_W = 2\pi\alpha M_s + (\alpha\eta - \beta)\mathbf{u}/\gamma\Delta. \quad (3)$$

In case (II) the time-average  $\langle \sin 2\psi \rangle \rightarrow 0$  in Eq. (1a). Neglecting terms of order  $\alpha^2$  and  $\alpha\beta$  with respect to 1,

$$\dot{\mathbf{q}}_{II} = \gamma \Delta \alpha H_a + \eta \mathbf{u}. \quad (4)$$

In this precessional regime, adiabatic torque alone augments the wall velocity. Adiabatic and nonadiabatic interac-

tions may thus be probed independently by using a field to select regime I or II via Eq. (3). To explore this, wall velocities  $v$  were measured in a  $20 \text{ nm} \times 600 \text{ nm}$   $\text{Ni}_{80}\text{Fe}_{20}$  nanowire (Fig. 2), using high-bandwidth Kerr polarimetry [12]. The  $v$ - $H$  curves of the left wall at  $\mathbf{j} = 0$  and  $\pm 5.8 \times 10^{11} \text{ A/m}^2$  are linear at low and high  $H$ , as expected from Eqs. (2) and (4), and exhibit a peak at  $H_W = 6 \text{ Oe}$  marking breakdown. The zero- $H$  data show an anomalous hump at intermediate  $H$ , which vanishes with  $\mathbf{j}$  and whose cause is currently under investigation. Here we focus on low and high  $H$ , where  $\mathbf{j}$  simply imparts a vertical shift to  $v(H)$ . Although Eqs. (2) and (4) predict symmetric shifts about the  $\mathbf{j} = 0$  curve, the data show a positive current is more effective at increasing  $v$  than a negative current is at decreasing  $v$ .

To explore the symmetries of the interaction,  $v(\mathbf{j})$  was measured at various constant  $H$ , and the symmetric ( $v_+$ ) and anti-symmetric ( $v_-$ ) components,  $v_{\pm}(\mathbf{j}) = (v(+\mathbf{j}) \pm v(-\mathbf{j}))/2$ , were determined. Results at  $H = 44 \text{ Oe}$  are shown in Fig. 2. The data reveal a linear component in  $\mathbf{j}$  with a nearly constant slope of  $\sim 2.7 \times 10^{-7} \text{ m}^3/\text{C}$  over the entire field range studied, and a nonlinear component that is quadratic at low and high  $H$ . We interpret the linear component within the model above, and find  $\alpha/\beta \approx \eta \approx 1$ . However, if the current characteristics are to be interpreted within this 1D model, then likewise must the field characteristics. Eqs. (2) and (4) predict the ratio of the slopes of  $v(H)$  above and below breakdown to be  $\alpha^2$ , or  $\sim 10^{-4}$ , compared to a measured value  $\sim 0.15$ . Adiabatic torque is an analog of the precessional damping that drives wall motion well above breakdown and leads to the high-field mobility. Since the 1D model fails by a factor  $10^3$  to describe the latter, it is questionable how well it describes the former.

Likewise, Eq. (3) defines a breakdown field dependent on the perpendicular anisotropy and current. We find no more than a  $\sim 10\%$  change in  $H_W$  over the current range studied, implying  $\alpha/\beta \approx \eta$ . However, Eq. (3) also predicts a zero- $\mathbf{j}$

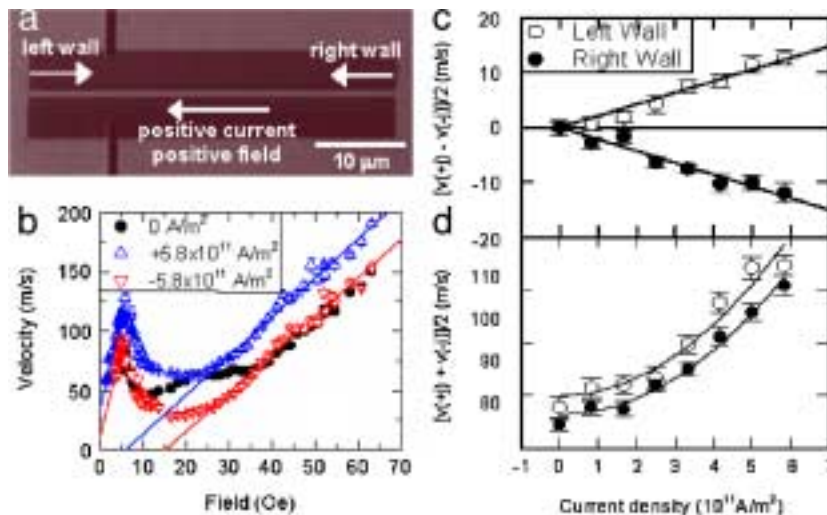


Fig. 2. (a) Plan-view SEM image of nanowire structure. For  $\mathbf{j} > 0$   $e^-$  flow to the right, (b) mobility curves of left wall for three currents. (c) Odd and (d) even  $v(\mathbf{j})$  components at  $H = 44$ .

breakdown field of  $\sim 50$  Oe, 10 times larger than the observed 6 Oe, at which the canting angle  $\psi$  is only  $\sim 4^\circ$ . Since the non-adiabatic component is analogous to a field, if the model fails to describe field-driven breakdown by an order of magnitude, it is questionable that variations in  $H_W$  can be reliably used to gauge the magnitude of  $\beta$ .

The failure of the 1D model to describe field-driven motion implies that its direct application to current-driven motion may be of limited value. Indeed, no 1D model has predicted the observed nonlinear component in  $v(j)$ , although its effect can exceed that of the linear component at moderate  $j$ . Meaningful comparison between experiment and theory will require models that fully account for realistic, time-variant domain structures, such as the vortex walls known to prevail in many experimental situations [13,14].

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